

# Physics

## Theory Part 12

Topics: Waves and Oscillation/ Electrodynamics

Course: B.Sc/ Physics

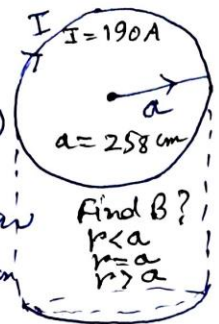
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Analogous to Gauss's law in E.F inside the cylinder (inflow) is zero. Analogy is the Ampere's law if we take Amperian loop inside of



(i) radius  $r < a$ , then it includes zero current, so

$$\int \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enc} = 0$$

$\Rightarrow B = 0 \forall r < a$ . i.e for  $r = 0 \text{ cm}, 1.20 \text{ cm}$ .

(ii) for  $r = a$ ,  $\int \vec{B} \cdot d\vec{\ell} = \mu_0 I_{enc}$ .

$$\text{or, } B \times 2\pi a = \mu_0 \times I_{enc}$$

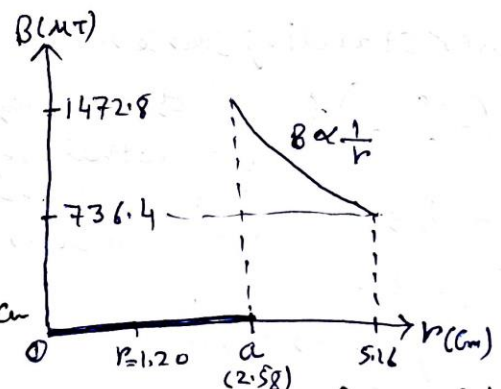
$$\text{or, } B = \frac{\mu_0 I_{enc}}{2\pi a} = \frac{4\pi \times 10^{-7} \times 190}{2\pi \times 2.58 \times 10^{-2}} = 147.28 \times 10^{-5} \text{ T}$$

(iii) For  $r > a$  also similar result will be obtained as  $I_{enc}$  is same only  $r$  changes

$$B \times 2\pi r = \mu_0 I_{enc} \quad \& \quad r = 5.16 \text{ cm}$$

$$\therefore B = \frac{\mu_0 I}{2\pi r} = \frac{4\pi \times 10^{-7} \times 190}{2\pi \times 5.16 \times 10^{-2}} = 73.64 \times 10^{-5} \text{ T}$$

So magnetic field inside the cylinder  $= 0$ , as  $I = 0$ . and outside,  $B \propto \frac{1}{r}$



Plot of  $B$  vs.  $r$  for cylindrical current carrying conductor

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wave eqn in 1D

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}; v = \frac{\omega}{k}$$

Given  $y = A \sin(kx + \omega t + \phi)$

$$\begin{aligned} \text{L.H.S} &= \frac{\partial^2 y}{\partial x^2} = \frac{\partial}{\partial x} \left( \frac{\partial y}{\partial x} \right) \\ &= \frac{\partial}{\partial x} [A k \cos(kx + \omega t + \phi)] \\ &= -A k^2 \sin(kx + \omega t + \phi) \quad \text{--- (1)} \end{aligned}$$

$$\begin{aligned} \text{R.H.S} &= \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2} = \frac{1}{v^2} \frac{\partial}{\partial t} \left( \frac{\partial y}{\partial t} \right) \\ &= \frac{1}{v^2} \frac{\partial}{\partial t} [A \omega \cos(kx + \omega t + \phi)] \\ &= \frac{1}{v^2} \times -A \omega^2 \sin(kx + \omega t + \phi) \\ &= \frac{k^2}{\omega^2} \times -A \omega^2 \sin(kx + \omega t + \phi) \\ &= -A k^2 \sin(kx + \omega t + \phi) \quad \text{--- (2)} \end{aligned}$$

Thus L.H.S = R.H.S from (1) & (2) so it is a solution.

From above it is clear that for the wave eqn,

$$\boxed{\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}}$$

solution (general) is

$$\boxed{y = A \sin(kx + \omega t + \phi) + B \cos(kx + \omega t + \phi)}$$

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EMAIL: RAJESH.NEOGY@GMAIL.COM**

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**Thanksss**